## Visualization of Two-way, Three-way and Higher Order Data Sets

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#### Data Order

- Data Order defined by the number of dimensions in which it is logically arranged
- Two-way: conventional data tables
  - Samples by variables
- Three-way: data cubes
  - EEM: Samples by excitation by emission
  - GC-MS: *Samples* by *retention* by *mass number*
  - Hyperspectral: *x* by *y* by *spectra*
- Four-way: series of data cubes
  - SIMS depth profiling: *x* by *y* by *z* by *spectra*
- Five-way: array of data cubes
  - EEM images: *sample* by *x* by *y* by *excitation* by *emission*



Etc.











#### Continued Refinement

#### PCA Scores of Arch Data





#### Issues With Larger Data Sets



Colorby Layered

Colorby Unsorted

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#### Translucent Data Points? Size?





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#### And There Are Limits





#### Visualizing Raw Data



#### Visualizing Preprocessing





#### Secondary Ion Mass Spectrometry (SIMS)





The primary ion source is moved over the sample surface in a pseudo-random pattern to obtain a hyperspectral image.



## Sputtering $\rightarrow$ Depth Profiling Sputter Ion Sputtering "peels off" a layer Beam, $C_{60}^{2+}$ exposing a new surface for hyperspectral imaging. Remove a Layer Layered Sample



## ToF-SIMS Imaging & Depth Profiling

- The primary beam is scanned over the surface
   mass channel spectrum (time of flight) at each pixel
  - 256x256 hyperspectral image of the surface
- Depth profiling is achieved by sputtering
   multiple hyperspectral images at 50 different depths (~200 nm depth profile)
- 256x256x406<sup>+</sup>x50 reduced to 85x85x300x50
   use mean of 3x3 windows, remove edge pixels, remove highest mass channels

 $^{\scriptscriptstyle +}406$  peaks were selected and integrated across all mass spectr



#### Data Analysis

- Principal Components Analysis (PCA)
  - orthogonal scores / loadings
- Multivariate Curve Resolution (MCR)
  - attempt to obtain pure component, non-negative scores and factors that are more physically interpretable
- Use Poisson scaling
  - allows lower signal (higher mass channels) to influence the model
- Parallel Factor Analysis (PARAFAC)



#### Example Image







#### PCA Results Tiled Scores





Image of Scores on PC 2 (16.81%)













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## Linking







### Visualizing 3-D Volume









As recovered

Preprocessing undone



#### Another take: PARAFAC

- Unfold 4-way data array in pixel (x-y) modes
  - 7225 pixels by 300 mass channels by 50 layers
- Use Parallel Factor Analysis to model data as outer product of the three modes
- Fold pixel mode back up to make images
- Used non-negativity constraint



#### PARAFAC Model

#### 88.1% Variance Captured!



22

21

20

19

18

17

16

15

14

13

12

Loadings First PARAFAC Component



Loadings Second PARAFAC Component



**PARAFAC Loadings for Depth Mode** 0.5 0.45 0.4 **bakafac** Loadings 0.3 0.2 0.2 0.2 0.1 0.05 0 20 30 10 15 25 35 40 5 45 50 Depth into Sample

Loadings Third PARAFAC Component





#### Pixel Factors Correlated!



- Variations in signal strength at each pixel persist as depth is profiled
- Seems to be 5 discrete signal strength levels
- Sampling problem??







# MATLAB® PLS\_Toolbox MIA\_Toolbox



#### Conclusions

- Many ways to look at data!
- "Color-by" especially useful on raw data or for adding info to other plots
- Factor based methods (PCA, MCR, PARAFAC, etc.) can condense data down to lower dimensions while retaining info
- Slicing and adding motion can reveal things previously un-noticed

